

# Optics for Engineers

## Chapter 10

Charles A. DiMarzio  
Northeastern University

Nov. 2012

# Coherent Sum

- Adding Fields (Chapter 7)

$$I = E_1^* E_1 + E_2^* E_2 + E_1^* E_2 + E_1 E_2^*$$

- Mach–Zehnder Interferometer

$$E_1(t) = E_s \left( t - \frac{z_1}{c} \right) \quad E_2(t) = E_s \left( t - \frac{z_2}{c} \right)$$

- Mixing Term: (Source,  $E_s(t) = E_0 e^{j\omega t}$ , with  $k = 2\pi/\lambda = \omega/c$ )

$$E_2 E_1^* = E_s(t - z_2/c) E_s^*(t - z_1/c) =$$

$$E_0(t - z_2/c) E_0^*(t - z_1/c) e^{j(\phi_2 - \phi_1)}$$

$$\phi_1 = kz_1 \quad \phi_2 = kz_2$$

# Irradiance of Coherent Sum

- Coherent Light as in Chapter 7

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos(\phi_2 - \phi_1)$$

- Visibility for Equal Irradiances

$$V = \frac{I_{max} - I_{min}}{I_{max} + I_{min}} = \frac{4I_1 - 0}{4I_1 + 0} = 1$$

- Random Source ( $E_0$  Varies Randomly)

$$\langle E_2 E_1^* \rangle = \langle E_0(t - z_2/c) E_0^*(t - z_1/c) \rangle e^{j(\phi_2 - \phi_1)}$$

$$\langle E_2 E_1^* \rangle = \langle E_0(t) E_0^*(t - \tau) \rangle e^{j(\phi_2 - \phi_1)} \quad \tau = \frac{z_2 - z_1}{c}$$

# Coherence

- Previous Result

$$\langle E_2 E_1^* \rangle = \langle E_0(t) E_0^*(t - \tau) \rangle e^{j(\phi_2 - \phi_1)} \quad \tau = \frac{z_2 - z_1}{c}$$

- Temporal Autocorrelation Function,  $\Gamma$

$$I = I_1 + I_2 + 2\Re \left[ \Gamma e^{j(\phi_2 - \phi_1)} \right] \quad \Gamma = \langle E_0^*(t - \tau) E_0(t) \rangle$$

- Visibility with  $I_1 = I_2$

$$V = \frac{I_{max} - I_{min}}{I_{max} + I_{min}} = \frac{2I_1(1 + |\Gamma|) - 2I_1(1 - |\Gamma|)}{2I_1(1 + |\Gamma|) + 2I_1(1 - |\Gamma|)}$$

$$V = \gamma = \frac{4|\Gamma|}{4I} = \frac{|\Gamma|}{I}$$

# Temporal Autocorrelation Function

- General Definition (See Previous Page)

$$\Gamma = \langle E_0^*(t - \tau) E_0(t) \rangle \quad \gamma(\tau) = \frac{\Gamma(\tau)}{|E_1 E_2^*|}$$

- Short Times: Equal (Or at Least Correlated) Fields

$$\Gamma = \langle E_1^*(t) E_1(t) \rangle$$

$$\gamma(\tau) \rightarrow 1 \quad \text{as} \quad \tau \rightarrow 0$$

- Long Time: Uncorrelated Fields

$$\Gamma = \langle E_1^*(t - \tau) E_1(t) \rangle = \langle E_1^*(t - \tau) \rangle \langle E_1(t) \rangle$$

$$\gamma(\tau) \rightarrow 0 \quad \text{as} \quad \tau \rightarrow \infty$$

# Coherent and Incoherent Addition

- Coherent Addition (*e.g.* Short Times)

$$E = E_1 + E_2 \quad I = |E|^2$$

- Incoherent Addition (*e.g.* Long Times)

$$\langle I \rangle = \langle I_1 \rangle + \langle I_2 \rangle \quad (\text{Incoherent Addition})$$

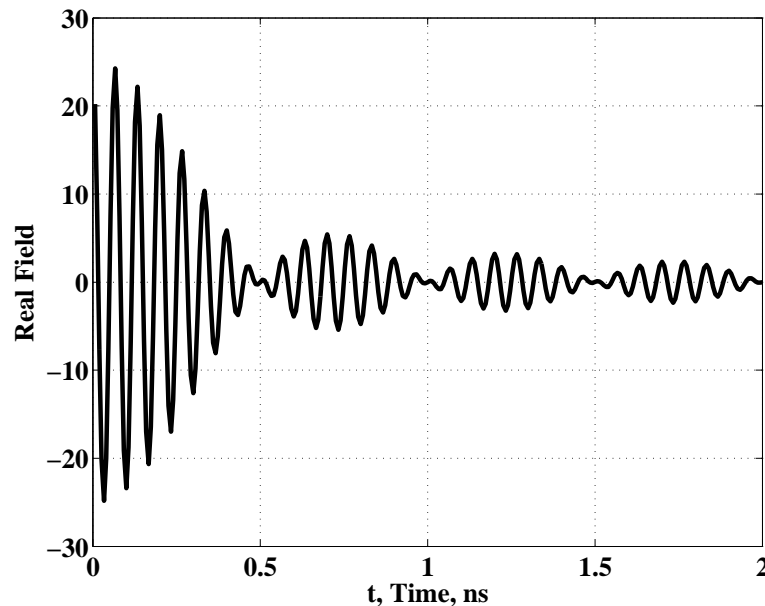
- Need to Quantify Times

# Digression: Mode-Locked Lasers

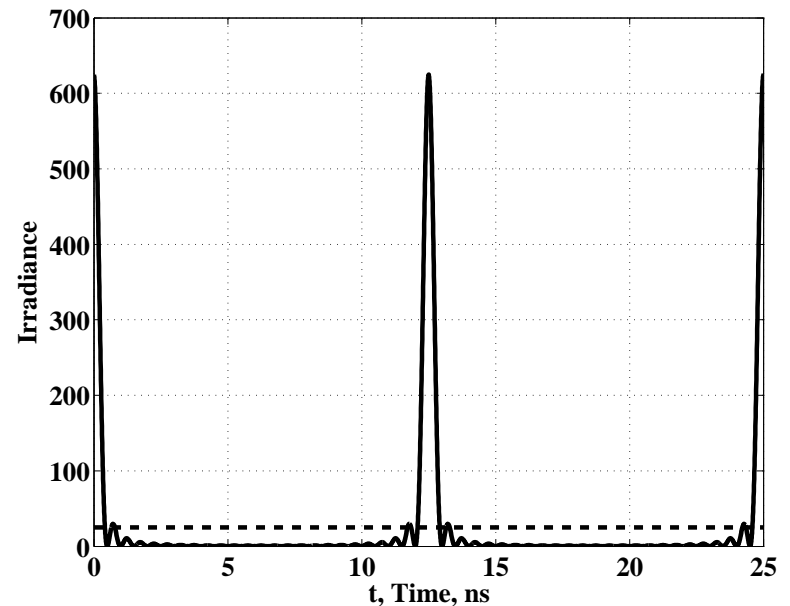
- Sum of Longitudinal Modes: e.g. 25 Modes

$$E = \sum_{m=-12}^{12} E_m = \sum_{m=-12}^{12} e^{i2\pi[f_{center} + m \times FSR]t}$$

- Transform-Limited Pulses Carrier Frequency Reduced for Clarity



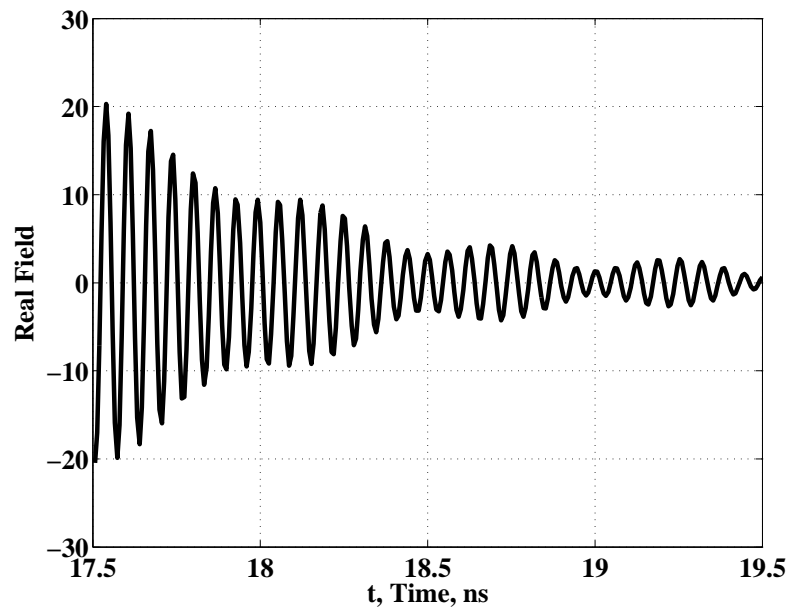
A. Mode-Locked Field



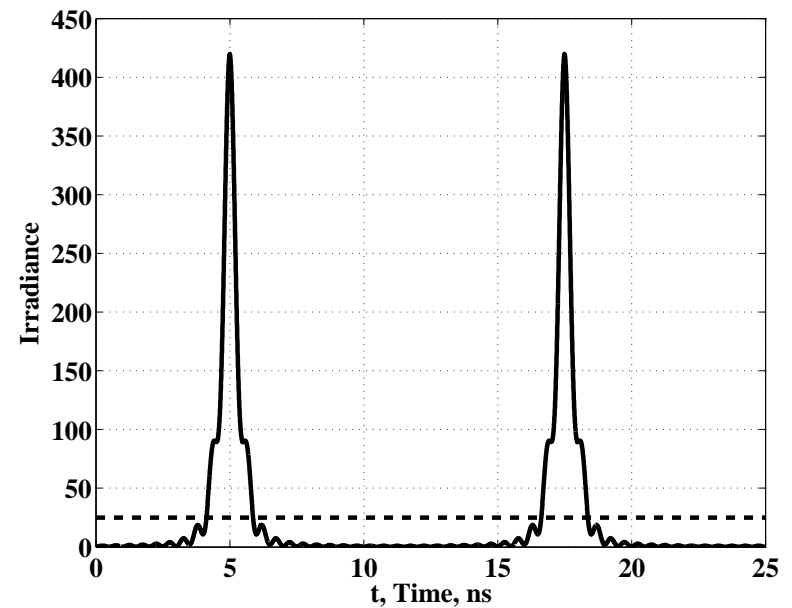
B. Mode-Locked Irradiance

# Pulse Dispersion

- Mode-Locked Laser Passing Through Glass
- “Chirped Pulses:” *e.g.*  $\frac{dt}{df} = -(1/3) \times 10^{-18} \text{sec/Hz}$
- Pulses Broadened in Time (Not Transform-Limited)



C. Chirped Field

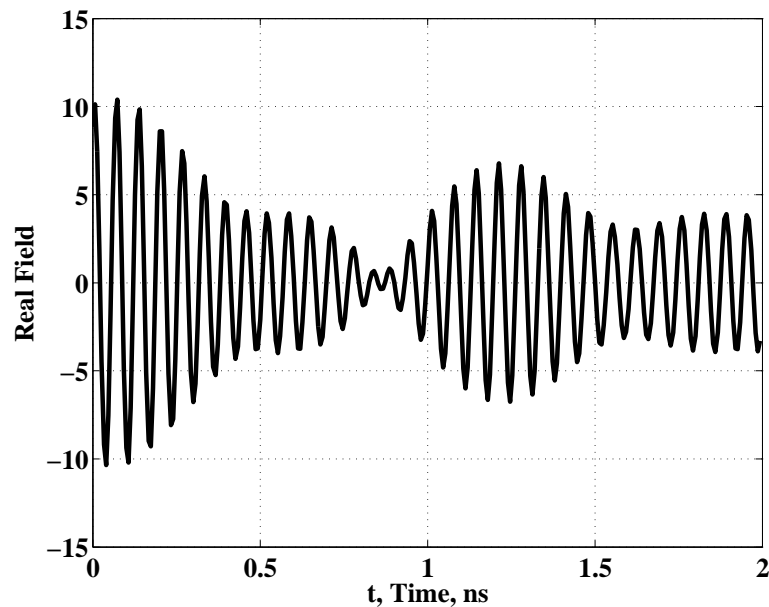


D. Chirped Irradiance

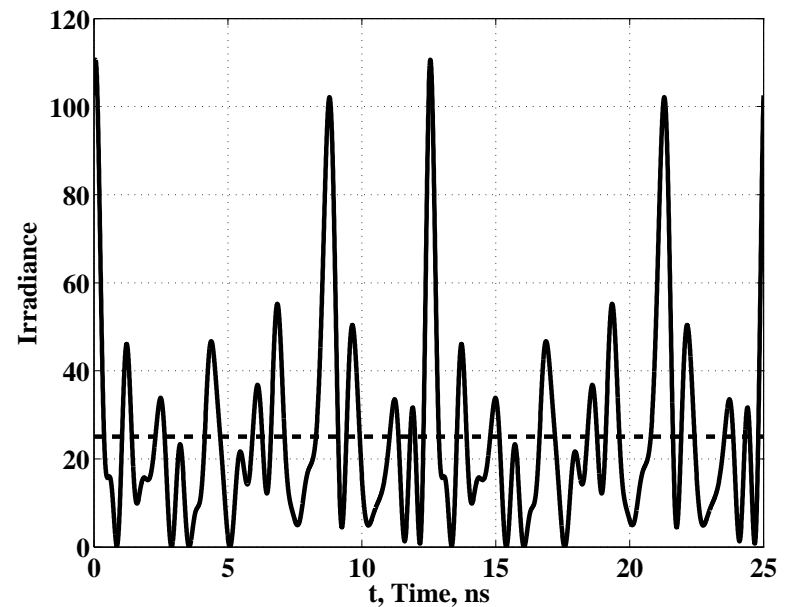


# Free-Running Multi-Mode Laser

- “Unlocked” Laser
- Random Output with No Predictable Pulses
- Occasional “Hot Pulse”



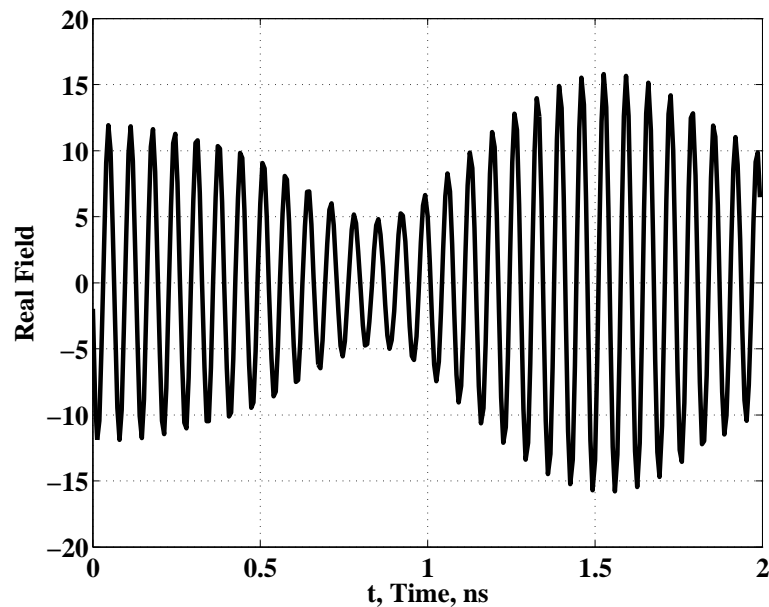
E. Unlocked Field



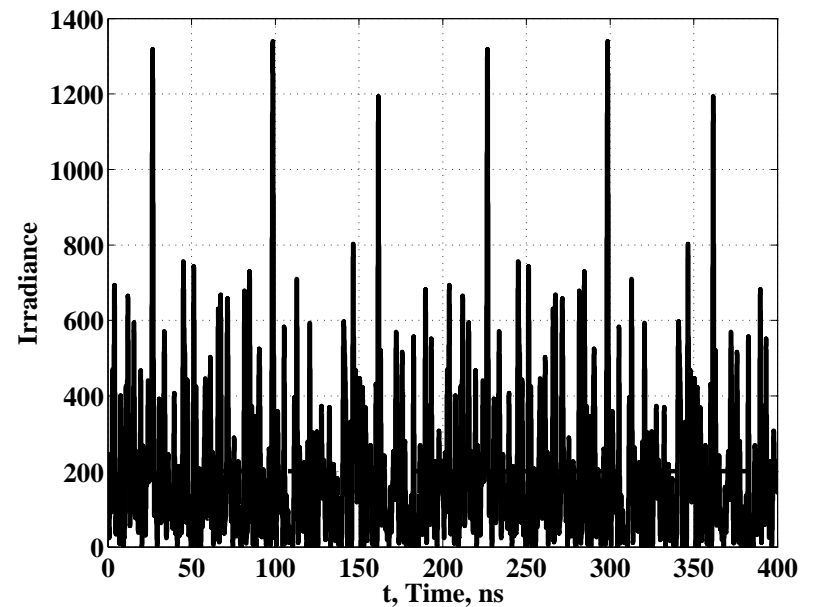
F. Unlocked Irradiance

# Multi-Mode Laser: Incoherent Addition

- 201 Modes 5MHz apart with Random Phases
- Short-Time Coherence ( $\ll 1/\text{Bandwidth}$ )



A. Field (Short Time)



B. Irradiance (Long Time)

# Temporal Coherence (1)

- Fourier Transforms

$$\tilde{E}(\omega) = \int_{-\infty}^{\infty} E(t) e^{-j\omega t} dt$$

$$E(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \tilde{E}(\omega) e^{j\omega t} d\omega$$

- Autocorrelation

$$\Gamma(\tau) = \langle E^*(t - \tau) E(t) \rangle$$

$$E(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \tilde{E}(\omega) e^{j\omega t} d\omega$$

$$E^*(t - \tau) =$$

$$\frac{1}{2\pi} \int_{-\infty}^{\infty} \tilde{E}^*(\omega') e^{-j\omega'(t-\tau)} d\omega'$$

- Combine and Simplify

$$\Gamma(\tau) = \left\langle \frac{1}{2\pi} \int_{-\infty}^{\infty} \tilde{E}^*(\omega') e^{-j\omega'(t-\tau)} d\omega' \dots \right.$$

$$\left. \frac{1}{2\pi} \int_{-\infty}^{\infty} \tilde{E}(\omega) e^{j\omega t} d\omega \right\rangle$$

$$\Gamma(\tau) = \left\langle \frac{1}{4\pi^2} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \dots \right.$$

$$\left. \tilde{E}^*(\omega') \tilde{E}(\omega) e^{j\omega'\tau} e^{j(\omega-\omega')t} d\omega' d\omega \right\rangle$$

- Exchange Average and Integrals

$$\Gamma(\tau) = \frac{1}{4\pi^2} \int_{-\infty}^{\infty} \dots$$

$$\left[ \int_{-\infty}^{\infty} \langle \tilde{E}^*(\omega') \tilde{E}(\omega) \rangle e^{j\omega'\tau} e^{j(\omega-\omega')t} d\omega' \right] d\omega$$

# Temporal Coherence (2)

- Previous Result

$$\Gamma(\tau) = \frac{1}{4\pi^2} \int_{-\infty}^{\infty} \left[ \int_{-\infty}^{\infty} \langle \tilde{E}^*(\omega') \tilde{E}(\omega) \rangle e^{j\omega'\tau} e^{j(\omega-\omega')t} d\omega' \right] d\omega$$

- Independent Sources with  $\langle \tilde{E}(\omega) \rangle = 0$

$$\langle E_m E_n^* \rangle = I_m \delta_{m-n} \quad (\text{Discrete})$$

$$\langle \tilde{E}^*(\omega') \tilde{E}(\omega) \rangle d\omega' = \tilde{I}(\omega') \delta(\omega - \omega') d\omega' \quad (\text{Continuous})$$

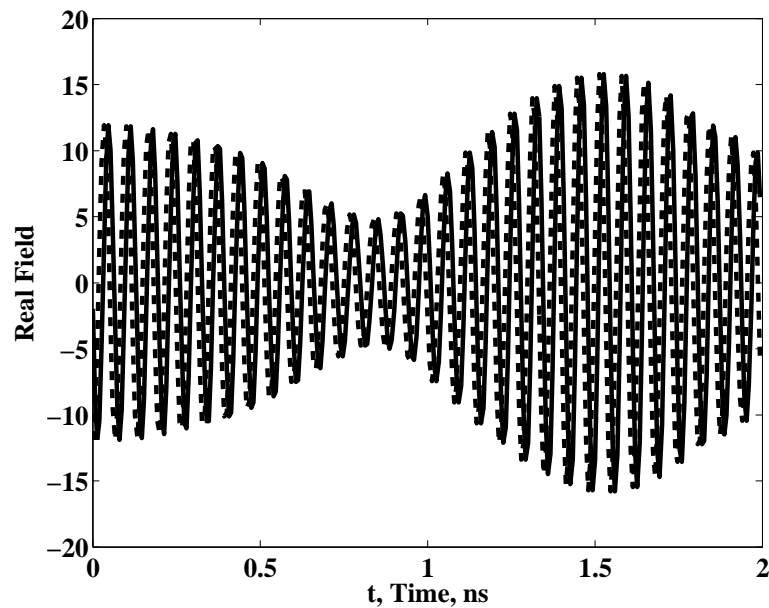
- Result

$$\left[ \int_{-\infty}^{\infty} \langle \tilde{E}^*(\omega') \tilde{E}(\omega) \rangle e^{j\omega'\tau} e^{j(\omega-\omega')t} d\omega' \right] = \tilde{I}(\omega) e^{j\omega\tau}$$

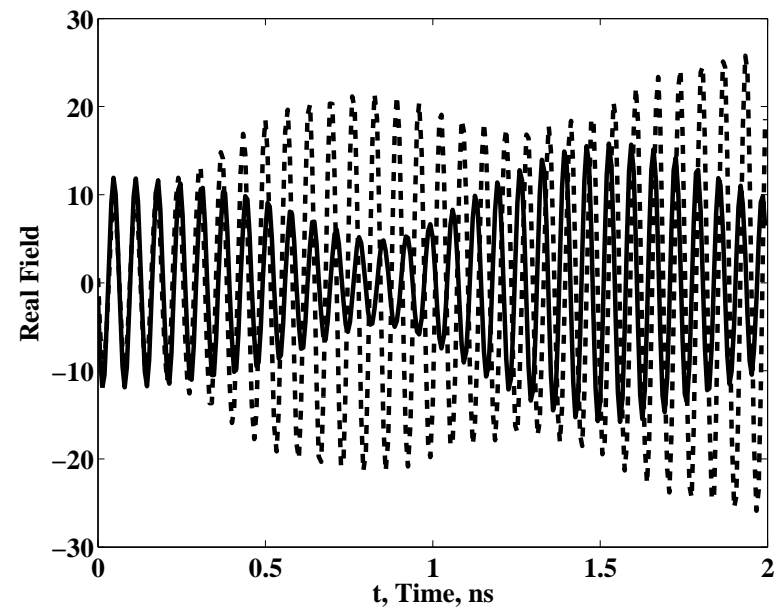
$$\Gamma(\tau) = \frac{1}{4\pi^2} \int_{-\infty}^{\infty} \tilde{I}(\omega) e^{j\omega\tau} d\omega \quad (\text{Weiner-Khintchine})$$

# Coherence in Interferometry

- Two Fields Shown (Solid and Dashed)
- Same Source with Different Time Delays
- Linewidth  $\approx 10\text{GHz}$



A. 10ps differential delay



B. 2ns differential delay

# Example: LED

- Wavelength Spectrum (Gaussian)

$$\lambda_0 = 635\text{nm} \quad \lambda_{FWHM} = 20\text{nm}$$

$$\left| \frac{\delta\lambda}{\lambda} \right| = \left| \frac{\delta f}{f} \right|$$

- Gaussian Fourier Transform Pair

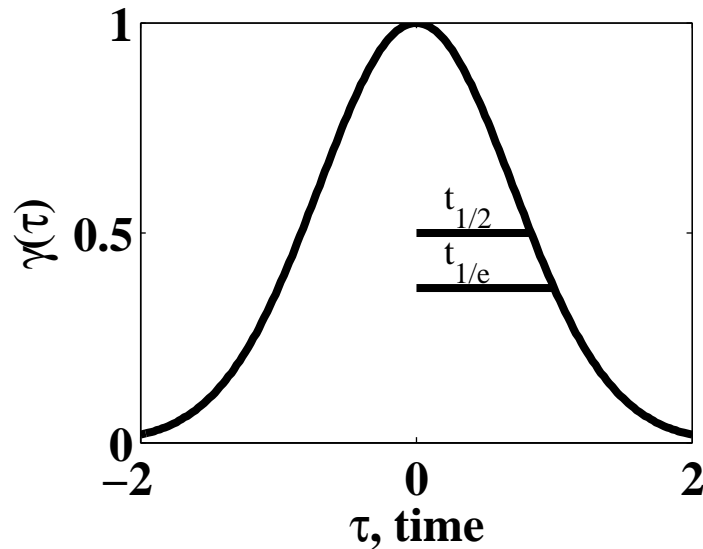
$$\gamma(\tau) = e^{-\left(t/t_{1/e}\right)^2} \quad \frac{2\sqrt{\pi}}{\omega_{1/e}} \tilde{\gamma}(\omega) = e^{-\left(\omega/\omega_{1/e}\right)^2}$$

- Convert Widths and Complete Calculation

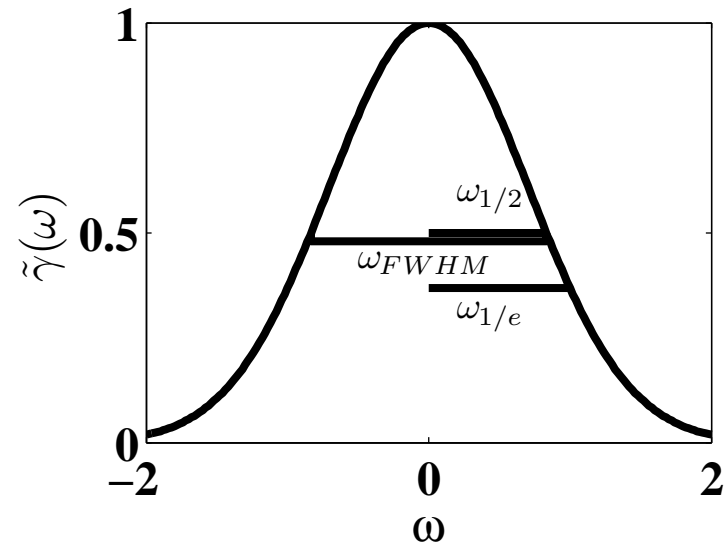
# Gaussian Widths Defined

$$e^{-\left(\omega_{1/2}/\omega_{1/e}\right)^2} = \frac{1}{2} \quad \text{at} \quad \omega_{1/2} = \sqrt{\ln 2} \omega_{1/e}$$

$$2\pi f_{1/2} = \omega_{1/2} = \sqrt{\ln 2} \omega_{1/e} \quad \omega_{1/e} = \frac{2\pi f_{1/2}}{\sqrt{\ln 2}}$$



A. Time Domain



B. Angular Frequency Domain

# LED Example Conclusion

$$t_{1/2} = \sqrt{\ln 2} \frac{2\sqrt{2}}{\omega_{1/e}} = \ln 2 \frac{2\sqrt{2}}{2\pi f_{1/2}} \approx \frac{0.31}{f_{1/2}} = \frac{0.62}{f_{FWHM}}$$

$$z_{1/2} = ct_{1/2}$$

$$\frac{z_{1/2}}{\lambda} = ft_{1/2} = \ln 2 \times \frac{2\sqrt{2}}{\pi} \frac{f}{f_{FWHM}} \approx 0.62 \frac{f}{f_{FWHM}}$$

$$\frac{z_{1/2}}{\lambda} \approx 0.62 \frac{f}{\delta f_{FWHM}} = 0.62 \frac{\lambda}{\lambda_{FWHM}}, \quad (\text{Gaussian Spectrum})$$

$$\frac{z_{1/2}}{\lambda} \approx 0.62 \times \frac{635}{20} \approx 20 \text{ Wavelengths} \quad z_{1/2} \approx 12.5 \mu\text{m}$$



# Laser vs. LED

- LED (Previous Page: Linewidth = 20nm)

$$\frac{z_{1/2}}{\lambda} \approx 0.62 \times \frac{635}{20} \approx 20 \text{ Wavelengths} \quad z_{1/2} \approx 12.5 \mu\text{m}$$

- HeNe Laser (30cm Coherence Length)

$$\frac{30 \times 10^{-2} \text{m}}{633 \times 10^{-9} \text{m}} \approx 4.7 \times 10^5 \approx 0.62 \frac{f}{f_{FWHM}} = 0.62 \frac{\lambda}{\lambda_{FWHM}}$$

$$f_{FWHM} = \frac{0.62f}{4.7 \times 10^5} = \frac{0.62c}{47 \times 10^6 \lambda} = 620 \times 10^6 \text{Hz}$$

$$\lambda_{FWHM} = \frac{0.62\lambda}{47 \times 10^5} = 830 \times 10^{-15} \text{m}$$

– Linewidth 620MHz or 830fm.

# Coherence in Beamsplitters

- Beamsplitter 5mm Thick ( $n = 1.5$ : OPD 75mm One Way)

$$\frac{z_{1/2}}{\lambda} = \frac{15 \times 10^{-3} \text{m}}{633 \times 10^{-9} \text{m}} = 23700 \approx 0.62 \frac{f}{f_{FWHM}} = 0.62 \frac{\lambda}{\lambda_{FWHM}}$$

$$\lambda_{FWHM} = \frac{0.62 \times 633 \text{nm}}{23700} = 16.6 \text{pm}$$

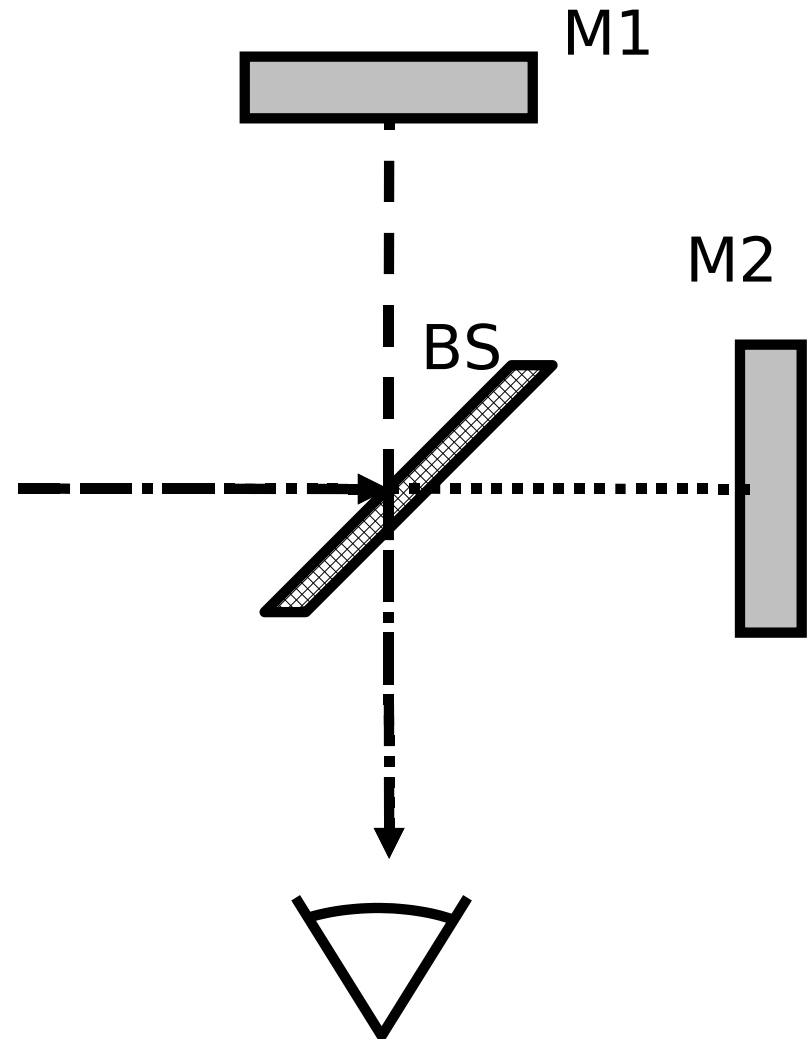
$$f_{FWHM} = \frac{0.62c}{23700\lambda} = 12.4 \text{GHz}$$

- Laser: Coherent Effects Produce Fringes
- LED:  $z_{1/2}$  Much Less than Thickness: No Fringes

# Optical Coherence Tomography

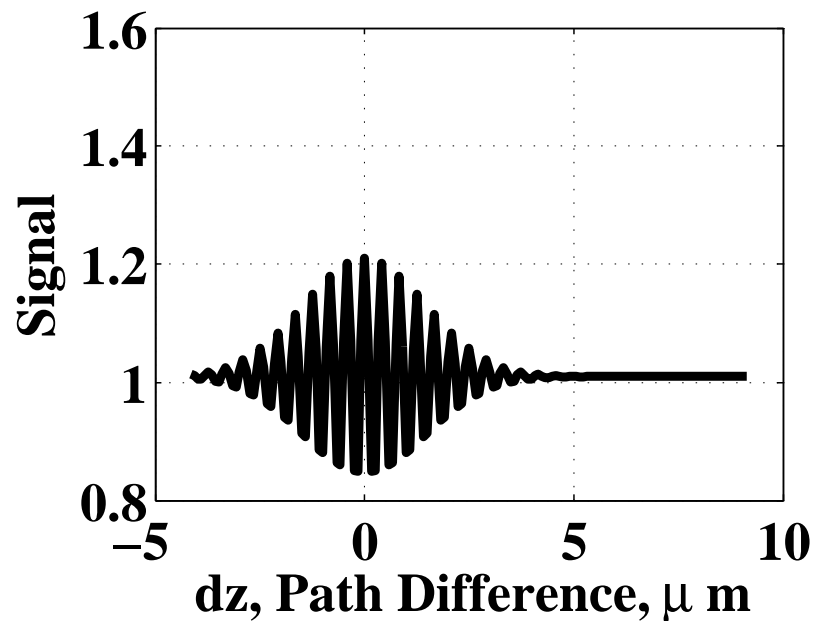
- Short Coherence Source
  - Super-Luminescent Diode
  - Ti:Sap Laser
  - Other
- $M1$  is Reference
- Moving Reference Mirror
- $M2$  is Target
- Interference? Compare...
  - Path Difference
  - Coherence Length

- Michaelson Interferometer

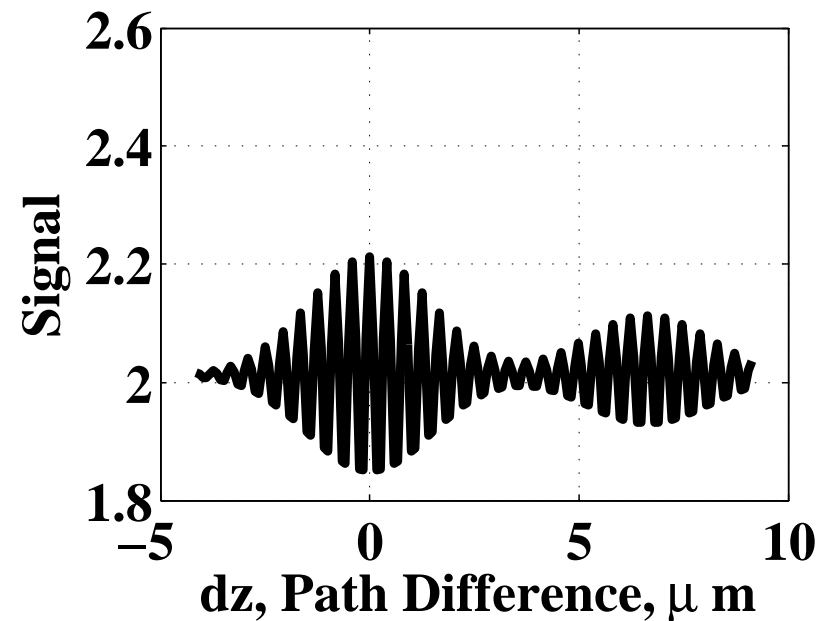


# OCT Signals

- Examples with Partial Reflectors
- Air–Glass Interfaces (Simulated Signals)
- Idea Extends to Thick “Distributed” Targets



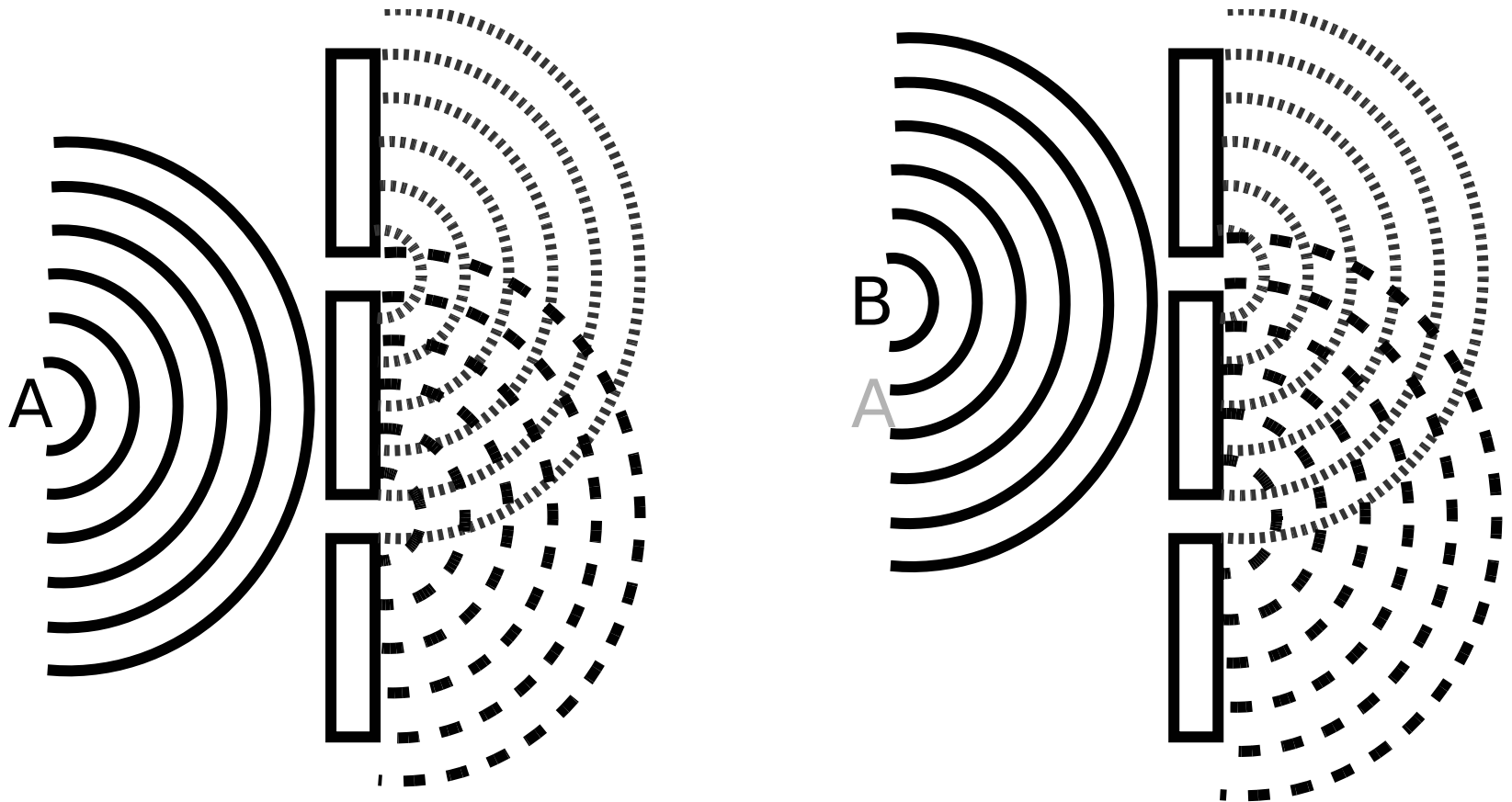
A. Target at Zero



B. Added target at  $8\mu\text{m}$

# Spatial Coherence

- Double Slit with Source at A Produces Diffraction Pattern
- Source at B Produces a Different Diffraction Pattern
- What about Both Together?



# Double Slit with Different Sources

- Sources Mutually Coherent

$$\langle |E_1^* E_2| \rangle = \sqrt{|E_1|^2 |E_2|^2}$$

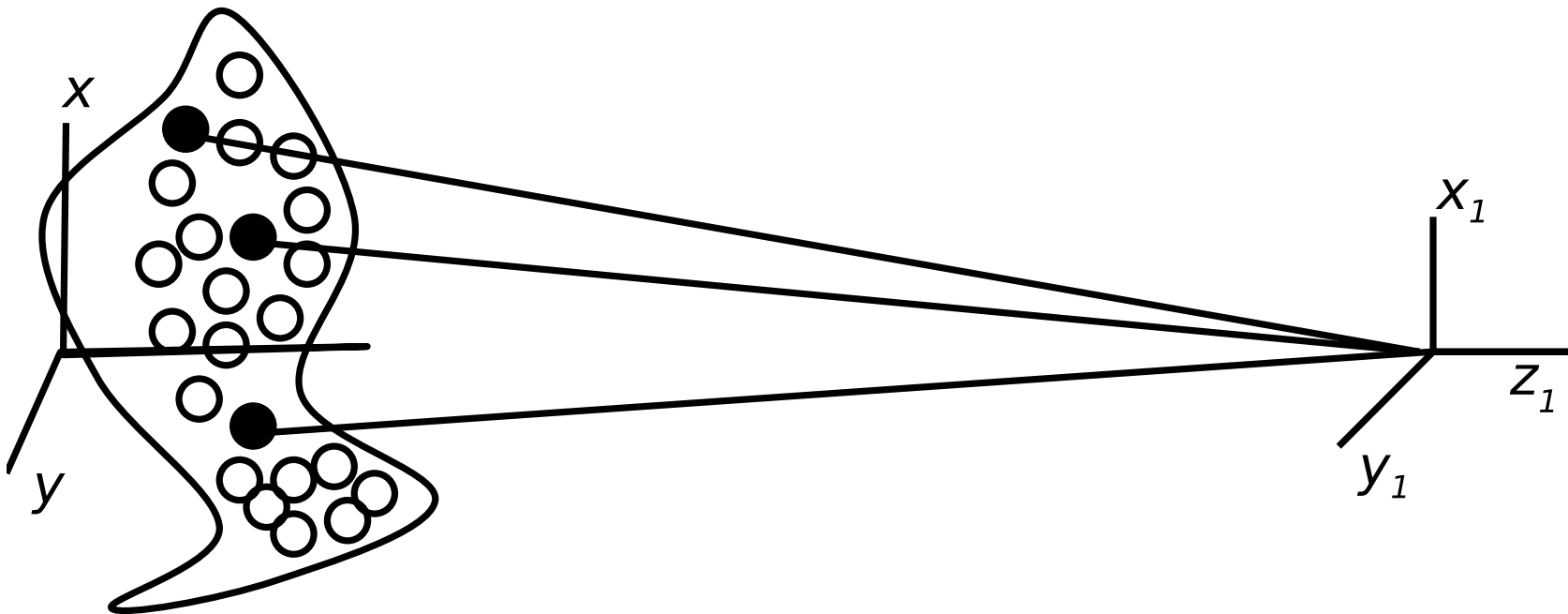
- Some Well-Defined Pattern with High Visibility

- Incoherent Sources

- Each Produces its Own Diffraction Pattern
- Peaks and Nulls in Different Places
- Ultimately Incoherent Addition

# Model for Spatial Coherence

- Multiple Point Sources
- Each Independent of the Others
- Compute Coherence Between  $(x_1, y_1, z_1)$ , and  $(x'_1, y'_1, z_1)$



# Van Cittert–Zernicke Theorem (1)

- Correlation

$$\Gamma(x_1, y_1, x'_1, y'_1) = \langle E^*(x'_1, y'_1, z_1) E(x_1, y_1, z_1) \rangle$$

- Fraunhofer Diffraction

$$E(x_1, y_1, z_1) = \frac{jk e^{jkz_1}}{2\pi z_1} e^{jk \frac{x_1^2 + y_1^2}{2z_1}} \iint E(x, y, 0) e^{jk \frac{x^2 + y^2}{2z_1}} e^{-jk \frac{xx_1 + yy_1}{z_1}} dx dy$$

$$E^*(x'_1, y'_1, z_1) = \frac{-jk e^{-jkz_1}}{2\pi z_1} e^{-jk \frac{(x'_1)^2 + (y'_1)^2}{2z_1}} \times$$

$$\iint E^*(x', y', 0) e^{-jk \frac{(x')^2 + (y')^2}{2z_1}} e^{+jk \frac{x'x'_1 + y'y'_1}{z_1}} dx' dy'$$



# Van Cittert–Zernicke Theorem (2)

- Combine Previous Equations

$$\Gamma(x_1, y_1, x'_1, y'_1) = \frac{-jke^{-jkz_1}}{2\pi z_1} e^{-jk\frac{(x'_1)^2 + (y'_1)^2}{2z_1}} \frac{jke^{jkz_1}}{2\pi z_1} e^{jk\frac{x_1^2 + y_1^2}{2z_1}} \times$$

$$\int \int \left[ \int \int \langle E^*(x', y', 0) E(x, y, 0) \rangle \times \right.$$

$$\left. e^{-jk\frac{(x')^2 + (y')^2}{2z_1}} e^{+jk\frac{x^2 + y^2}{2z_1}} e^{+jk\frac{x'x_1 + y'y_1}{z_1}} e^{-jk\frac{xx_1 + yy_1}{z_1}} dx' dy' \right] dx dy$$

- Simplification:  $x^2 - (x')^2 = (x + x')(x - x')$

$$\Gamma(x_1, y_1, x'_1, y'_1) = \frac{-jke^{-jkz_1}}{2\pi z_1} e^{jk\frac{(x'_1)^2 + (y'_1)^2}{2z_1}} \frac{jke^{jkz_1}}{2\pi z_1} e^{-jk\frac{x_1^2 + y_1^2}{2z_1}} \int \int \times$$

$$\left[ \int \int \langle E^*(x', y', 0) E(x, y, 0) \rangle e^{jk\frac{(x'+x)(x'-x) + (y'+y)(y'-y)}{2z_1}} e^{jk\frac{(xx_1 - x'x'_1) + (yy_1 - y'y'_1)}{z_1}} dx' dy' \right] dx dy$$

# Van Cittert–Zernicke Theorem (3)

- Random Phases:  $\langle E \rangle = 0$

$$\langle E^* (x', y', 0) E (x, y, 0) \rangle = 0$$

- Analogy with Wiener–Khinchine Theorem Earlier

$$\langle E^* (x', y', 0) E (x, y, 0) \rangle dx' dy' = I (x, y, 0) \delta (x - x') \delta (y - y') dx' dy'$$

$$\Gamma(x_1, y_1, x'_1, y'_1) = \frac{-jk e^{-jkz_1}}{2\pi z_1} e^{jk \frac{(x'_1)^2 + (y'_1)^2}{2z_1}} \frac{jk e^{jkz_1}}{2\pi z_1} e^{-jk \frac{x_1^2 + y_1^2}{2z_1}} \iint \times$$

$$\left[ \iint I(x, y, 0) \delta(x - x') \delta(y - y') e^{jk \frac{(xx_1 - x'x'_1) + (yy_1 - y'y'_1)}{z_1}} dx' dy' \right] dx dy$$

# Van Cittert–Zernicke Theorem (4)

- Outer Integral

$$\Gamma(x_1, y_1, x'_1, y'_1) = \frac{-jk e^{-jkz_1}}{2\pi z_1} e^{jk \frac{(x'_1)^2 + (y'_1)^2}{2z_1}} \frac{jk e^{jkz_1}}{2\pi z_1} e^{-jk \frac{x_1^2 + y_1^2}{2z_1}} \times$$

$$\int \int I(x, y, 0) e^{jk \frac{x(x_1 - x'_1) + y(y_1 - y'_1)}{z_1}} dx dy$$

- Simplify

$$\Gamma(x_1, y_1, x'_1, y'_1) = \left( \frac{k}{2\pi z_1} \right)^2 e^{jk \frac{(x'_1)^2 + (y'_1)^2}{2z_1}} e^{-jk \frac{x_1^2 + y_1^2}{2z_1}} \times$$

$$\int \int I(x, y, 0) e^{jk \frac{x(x_1 - x'_1) + y(y_1 - y'_1)}{z_1}} dx dy$$

# Van Cittert–Zernicke Theorem (5)

- Define Coordinate Differences

$$\xi = x'_1 - x_1 \quad \eta = y'_1 - y_1$$

- Van Cittert–Zernicke Theorem

$$\Gamma(\xi, \eta) = \left( \frac{k}{2\pi z_1} \right)^2 \iint I(x, y, 0) e^{jk \frac{x\xi + y\eta}{z_1}} dx dy$$

- Equation Similar to Fraunhofer Diffraction...

$$E(x_1, y_1, z_1) = \frac{jk e^{jkz_1}}{2\pi z_1} \iint E(x, y, 0) e^{-jk \frac{(xx_1 + yy_1)}{z_1}} dx dy$$

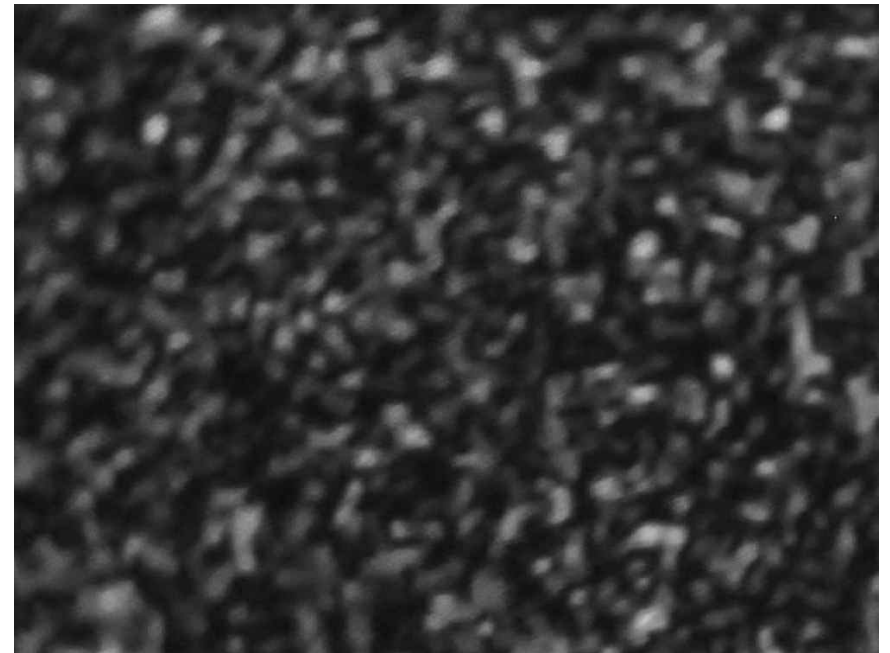
- ... but New Meaning (Coherence rather than Field)

# Spatially Coherent and Incoherent Illumination

$$\begin{array}{llll} E(x, y, 0) & \rightarrow & \text{Fraunhofer} & \rightarrow & E(x_1, y_1, z_1) \\ I(x, y, 0) & \rightarrow & \text{vC-Z} & \rightarrow & \Gamma(x_1 - x'_1, y_1 - y'_1) \text{ at } z_1 \end{array}$$



A. Spatially Coherent  
(Laser Source Direct)



B. Spatially Incoherent  
(Same Size Laser Source  
on Ground Glass)

# Coherent and Incoherent Source: Calculation

- Coherent Source  
(1mm HeNe Viewed at 5m)
  - Beam Size  $d$  at Receiver
- Spatially Incoherent Source  
(Same Laser on Ground Glass)
  - Whole Field Illuminated
  - Bright and Dark Regions
  - Diameter of  $\Gamma$  is  $d$
  - “Typical Spot Size:”  $d$

- Spatially and Temporally Incoherent  
Source: Filtered Tungsten 400 to 800nm
  - Whole Field Illuminated
  - Bright and Dark Regions Only for Short Times

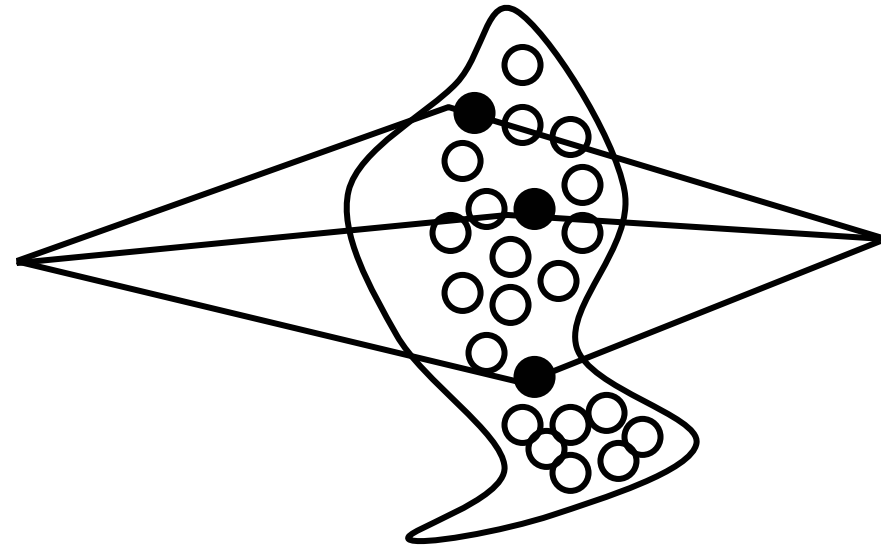
$$\frac{\delta\lambda}{\lambda} = \frac{\delta f}{f} \rightarrow 1$$

- Uniform when Measured for Longer than a Cycle (femtoseconds)

$$d = \frac{4\lambda}{\pi D} z = \frac{4 \times 633 \times 10^{-9} \text{m}}{\pi \times 10^{-3} \text{m}} 5 \text{m} = 4 \times 10^{-3} \text{m}$$

# Speckle in Scattered Light

- Coherent Source
  - Focused or Diverging
  - Spatially Coherent
  - Temporally Coherent
- Scattering Particles
  - Secondary Sources
  - Randomly Distributed
  - Illuminated by Source



- Large Illumination Pattern: Small Speckles
- Small Illumination Pattern: Large Speckles
- Infer Size of Illumination by Size of Speckles?
  - See Next Page

# Example: Finding the Focus

- Example ( $NA = 0.25$ ): Waist

$$d_0 = \frac{4\lambda}{\pi d} z \quad d_0 = \frac{2\lambda}{\pi NA}$$

$$d_0 = \frac{2532 \times 10^{-9} \text{m}}{\pi \cdot 0.25} = 1.4 \times 10^{-6} \text{m}$$

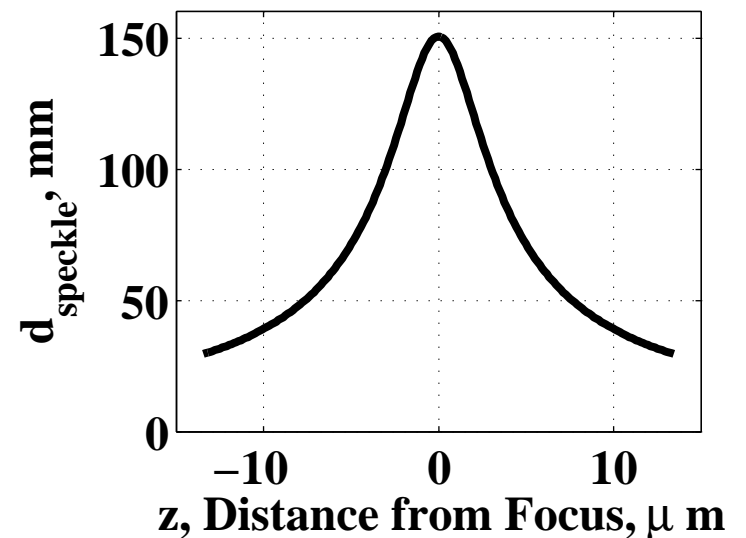
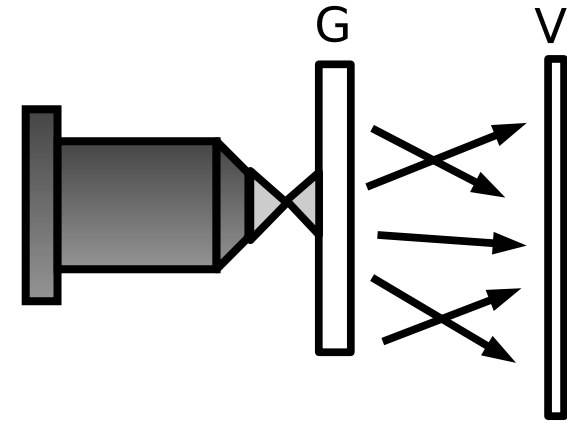
- At Glass

$$d_{\text{glass}} = d_0 \sqrt{1 + \frac{z^2}{b^2}} \quad b = \frac{\pi d_0^2}{4\lambda}$$

- Speckle Size

$$d_{\text{speckle}} = \frac{4\lambda}{\pi d_{\text{glass}}} z$$

– Same as Field of Coherent Source of Size  $d_{\text{glass}}$





# Example: Speckle in Laser Radar

- Carbon Dioxide Laser
  - $\lambda = 10.59\mu\text{m}$
  - $d_0 = 30\text{cm}$
  - Rayleigh Range

$$b = \pi d_0^2 / (4\lambda) = 6.7\text{km}$$

- Diameter at Target

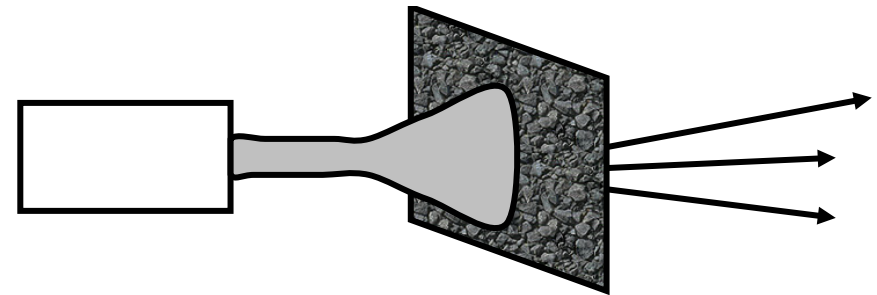
$$d_{\text{target}} = d_0 \sqrt{1 + \frac{z_t^2}{b^2}}$$

- Far Field  $z_t = 20\text{km}$

$$d_{\text{target}} \approx 90\text{cm}$$

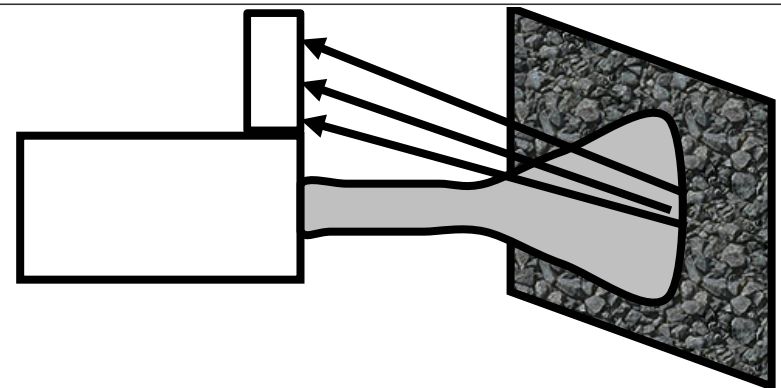
- Speckle Size at Receiver

$$\frac{4}{\pi} \frac{\lambda}{d_{\text{target}}} z_r = 15 \times 10^{-6} \text{rad} \times z_r$$



- Coaxial System  $z_r = z_t$  and Target in Far-Field

$$d_{\text{speckle}} = \frac{4}{\pi} \frac{\lambda}{\frac{4}{\pi} \frac{\lambda}{d_0} z} z = d_0$$



# Speckle Decorrelation

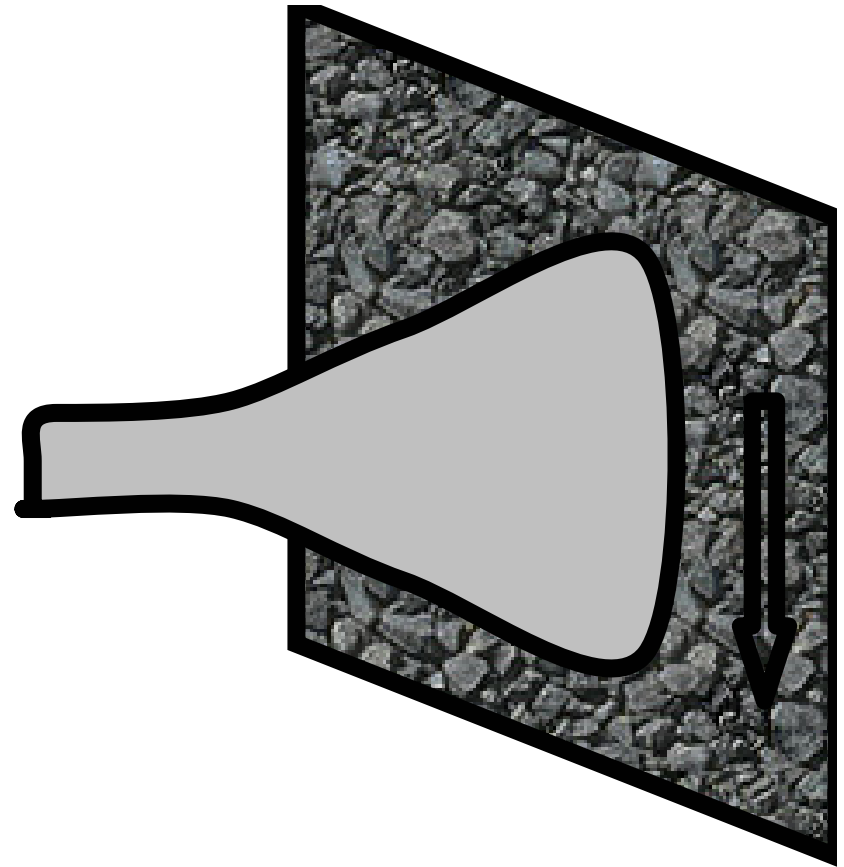
- Transverse Motion
  - New Scatterers
  - New Speckle Pattern
- Time on Target (ToT)

$$t_{target} = \frac{d_{target}}{v_{\perp}}$$

$$B_{tot} = \frac{v_{\perp}}{d_{target}}$$

- Recall Doppler Shift

$$f_{DR} = \frac{2v_{\parallel}}{\lambda}$$



# Speckle Reduction

- Average  $n$  Measurements
  - Improvement with  $1/\sqrt{n}$
  - Stationary Process
- Temporal Averaging

$$\sigma = \sqrt{\frac{t_{target}}{T_{integration}}}$$

- Long Time
  - Reduced Fluctuation  
but ...
  - ... More Target  
Variation
- “Matched Filtering”

- Area Averaging
  - Incoherent Averaging
  - Space-Invariant Process
- Aperture Averaging

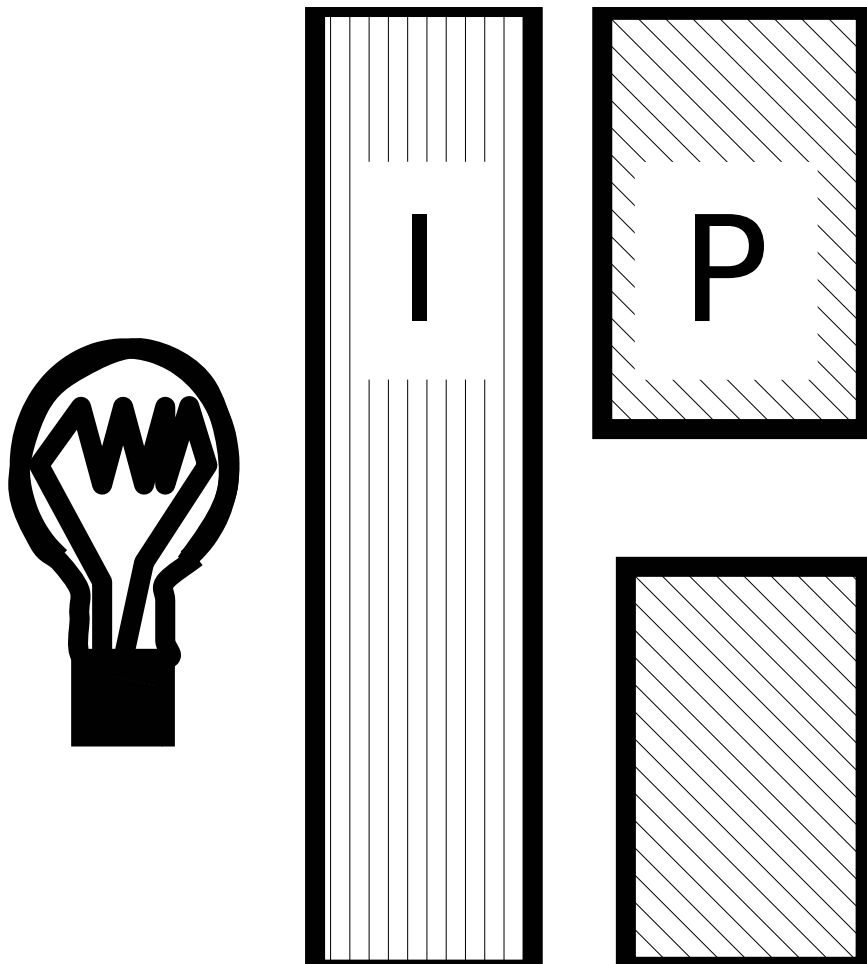
$$\sigma = \sqrt{\frac{A_{tx}}{A_{rx}}} = \frac{D_{tx}}{D_{rx}}$$

- Coherent Averaging Not Effective

$$\langle E \rangle = 0$$

- Other Diversity
  - Wavelength
  - Polarization

# Making Light Coherent



- Interference Filter
  - Dielectric Stack
  - Narrow Bandpass
  - Temporal Coherence

$$\frac{\lambda}{\delta\lambda} = \frac{\delta z}{\lambda}$$

- Pinhole
  - Unresolved
  - Spatial Filter
  - Narrow Spatial Bandpass
  - Spatial Coherence

# Making Light Incoherent

- Ground Glass Reduces Spatial Coherence
- Moving it Reduces Temporal Coherence

